

# Trapping and Escape of Buoyant Plumes in Stratified Water

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Close Collaboration with **Roberto Camassa** and **Brian White**

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**former grads:** Joyce Lin (Utah), Nick Moore (NYU), Z. Lin (IMA, Zhejiang Univ.)

**current grad:** Claudia Falcon, Chung-Nan Tzou, Claudio Viotti, Duo Zhao

**undergrads:** Johnny Reis, Robert Overman, Bailey Watson, Casey Smith,  
David Nenon

## Thanks to NSF:

NSF RTG DMS-0502266

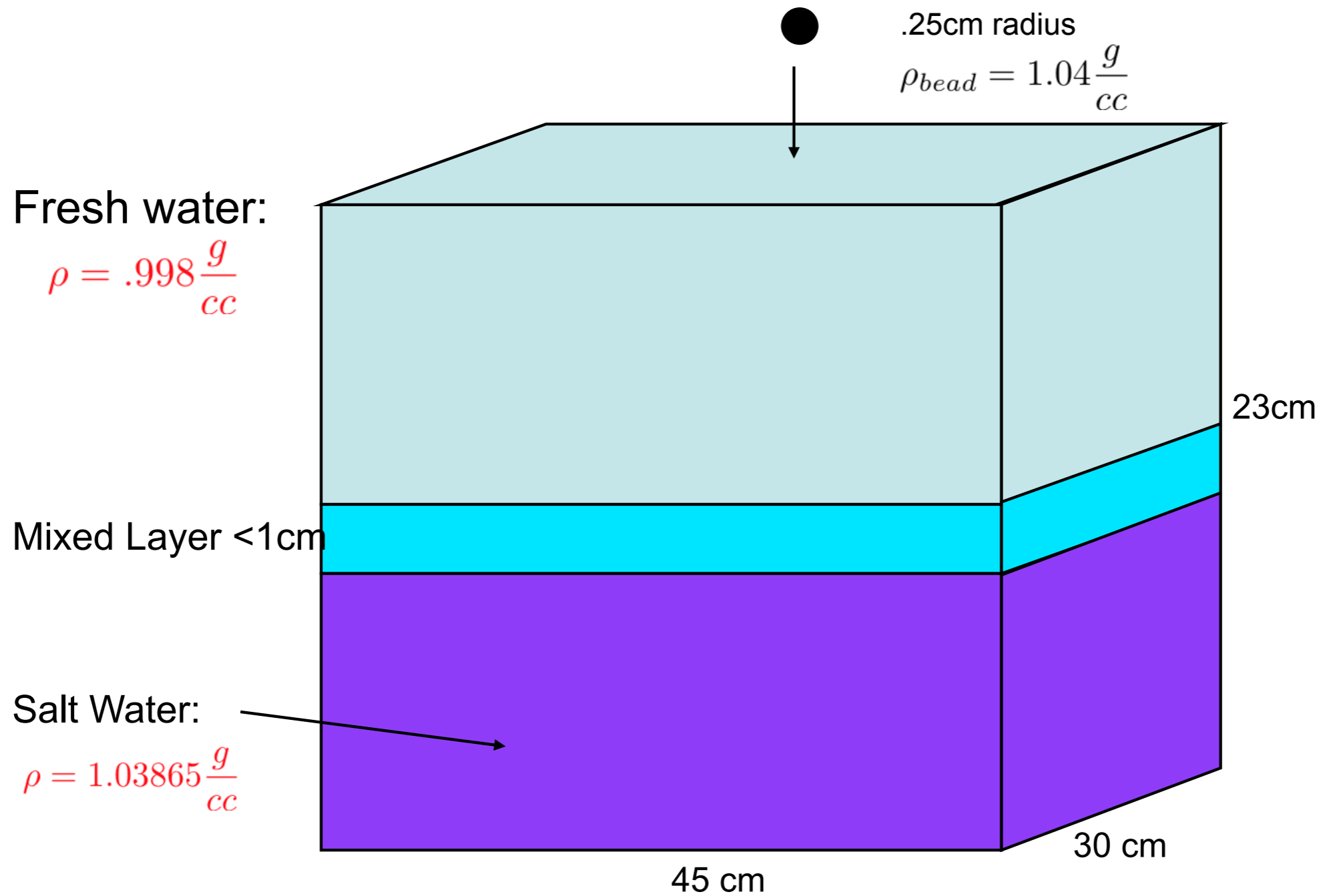
NSF RTG DMS-0943851

NSF RAPID CBET-1045653

NSF CMG ARC-1025523

NSF DMS- 1009750

# Experiment: Jets/Spheres in Stratified Fluids



# Internal Splash

- 1.0396 g/  
cc
- Stratified
- Sphere  
heavier  
than fluid  
at all  
depths
- Fast  
Playback
- $Re=300$

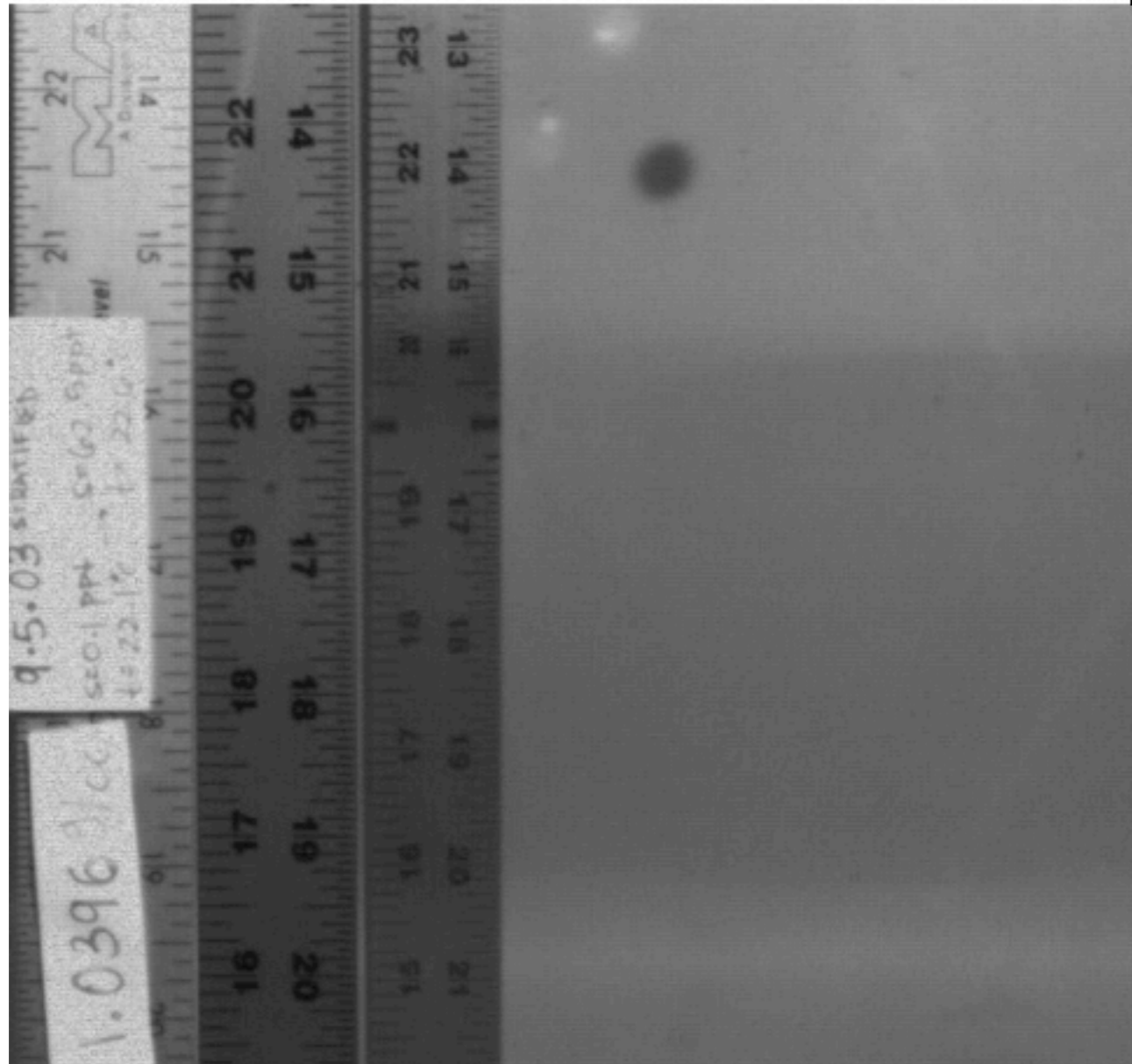
Abaid, Adalsteinsson, Agyapong, McL Phys of Fluids 2004

Srdic-Mitrovic, Mohamed, Fernando, JFM 1999 (no bounce)

1.0385g/cc

**For keynote with movies: See**  
**[pink-lady.amath.unc.edu/~rmm/sost](http://pink-lady.amath.unc.edu/~rmm/sost)**

# Internal Splash



- 1.0396 g/cc
- Stratified
- Sphere heavier than fluid at all depths
- Fast Playback
- $Re=300$

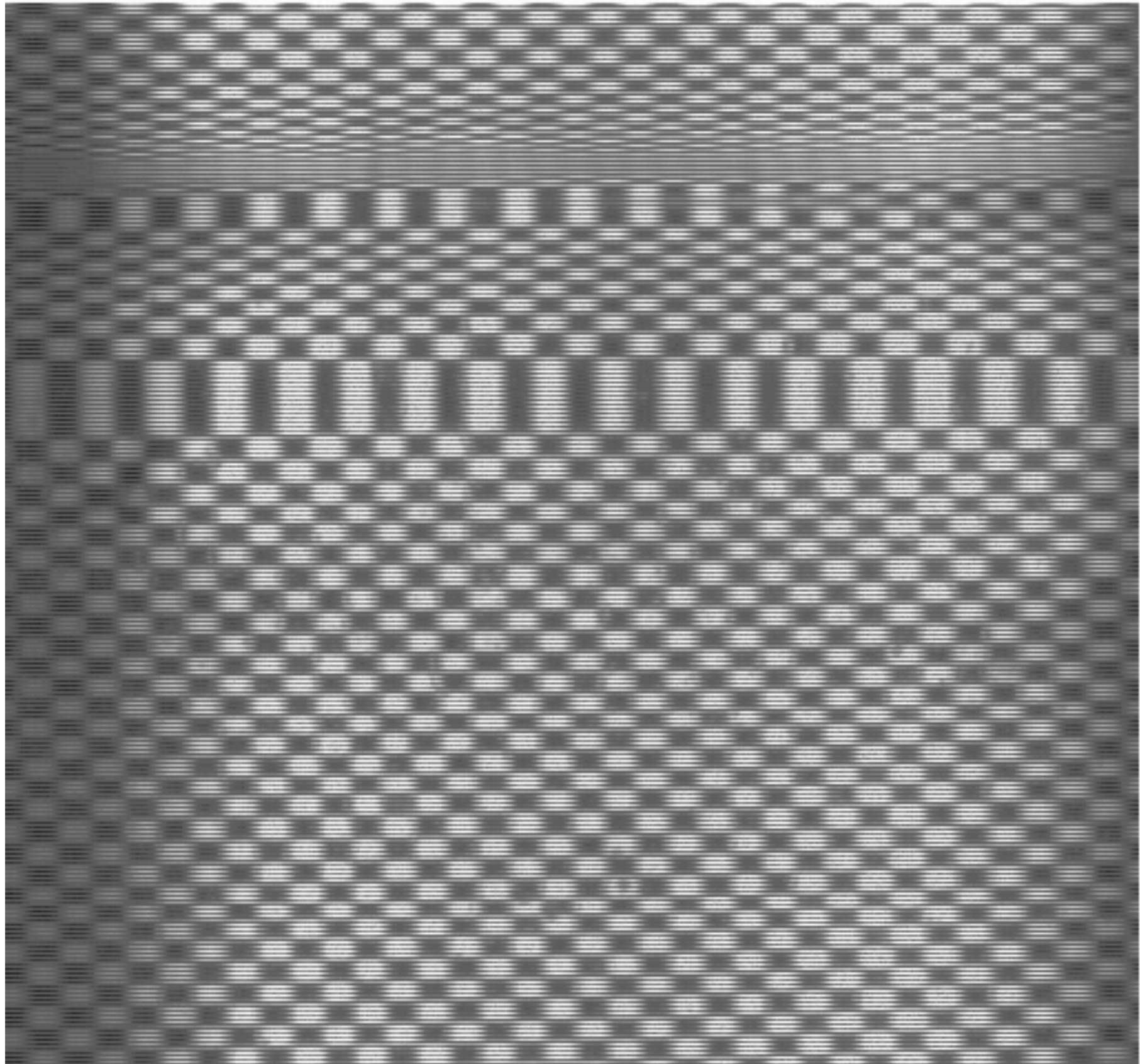
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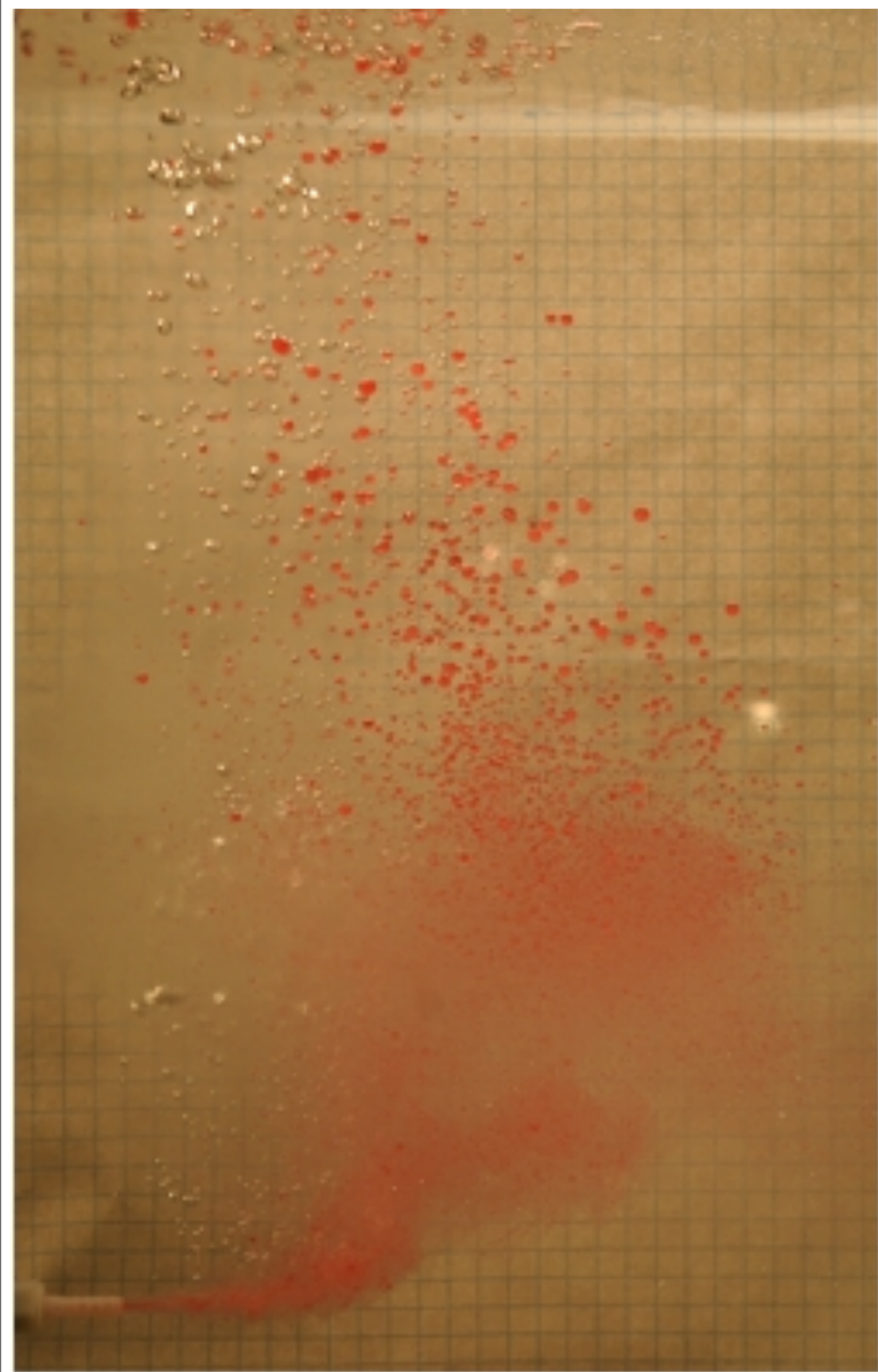


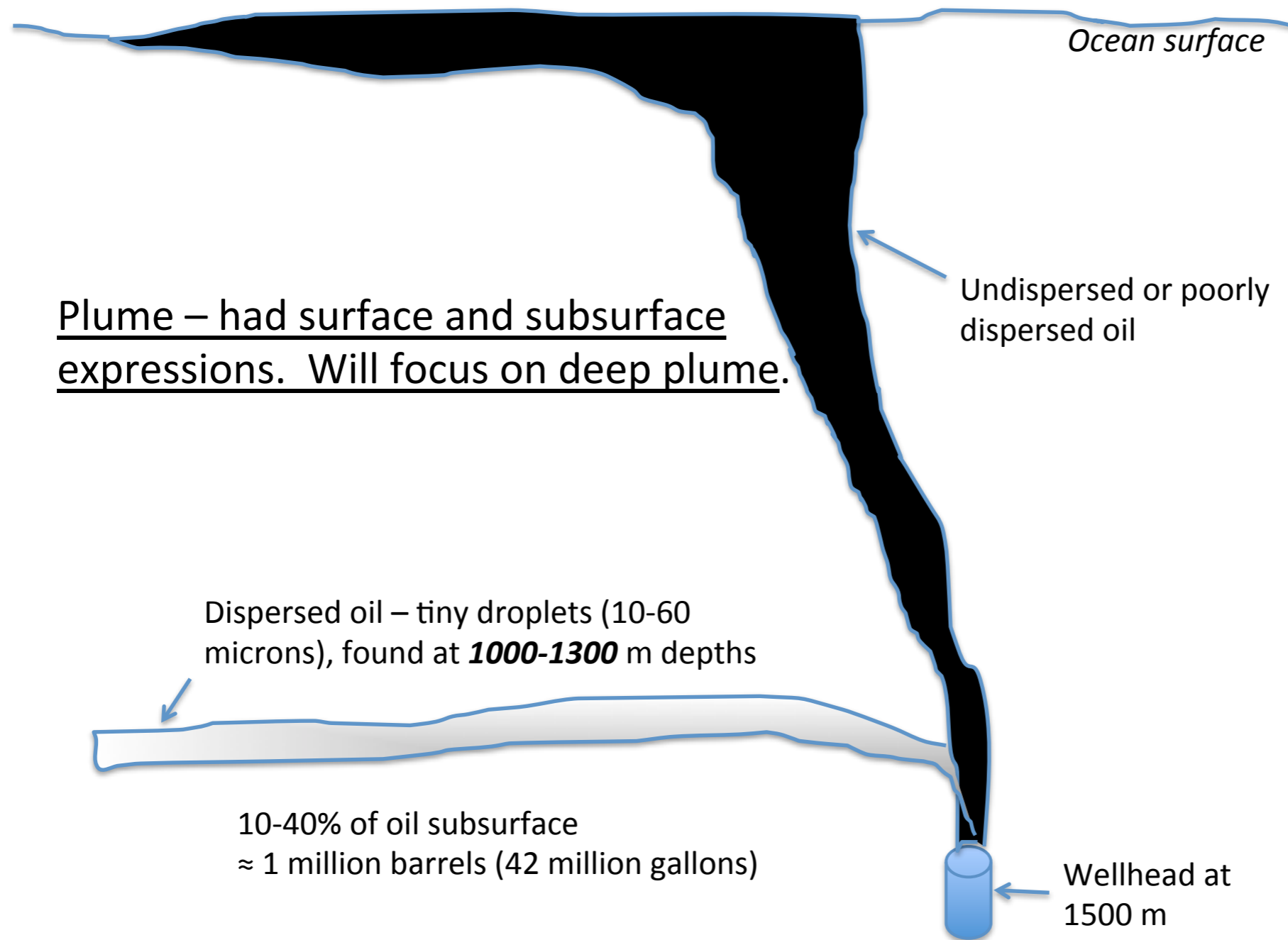
Left: low speed untreated oil, right: high speed+dispersant

Left: low speed untreated oil, right: high speed+dispersant





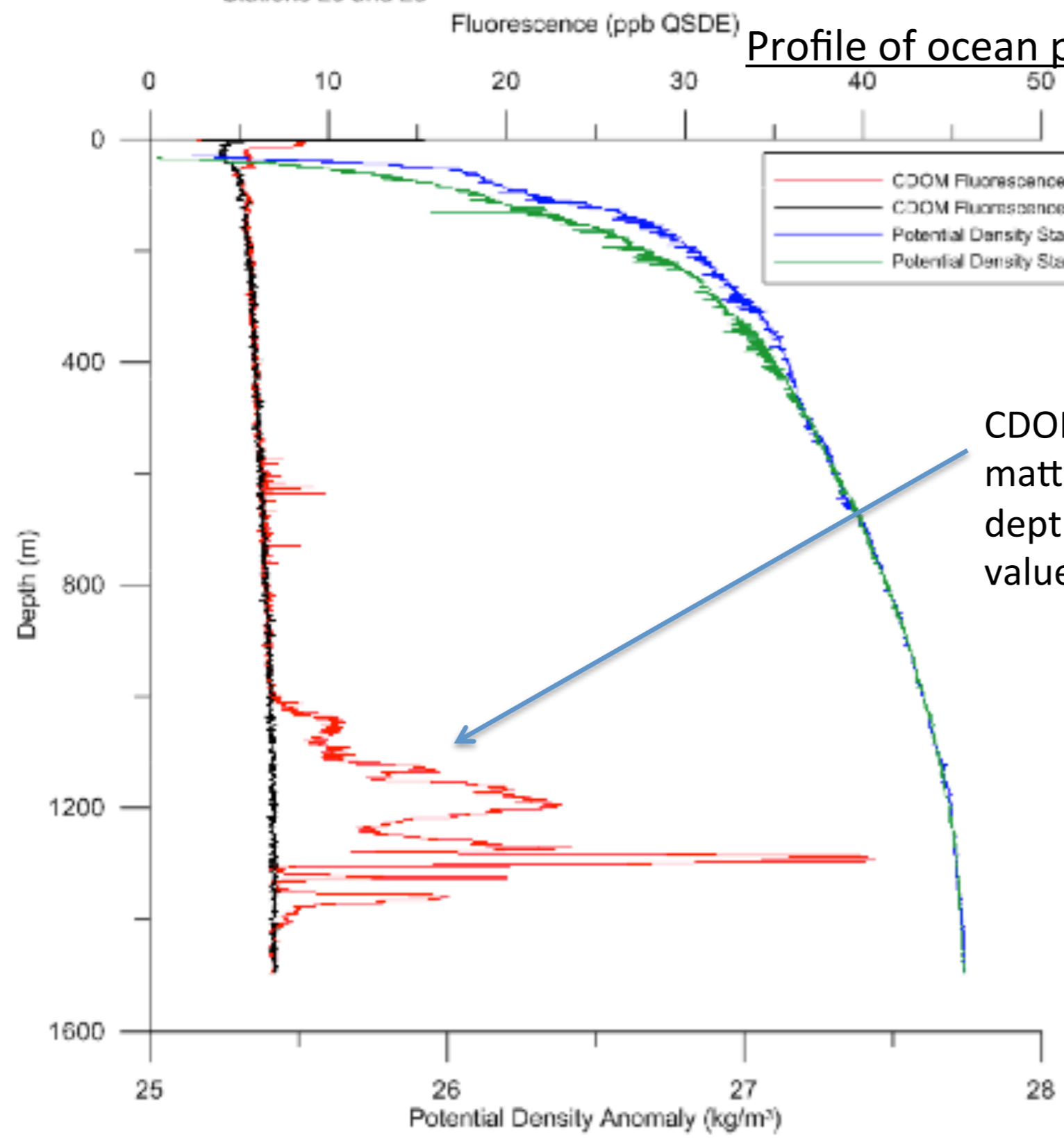




Slide: from **Harvey Seim,**  
**Marine Sciences, UNC**

Comparison of CDOM Fluorescence and Potential Density  
RV Brooks-McCall -- Cruise 2 - May 15-17, 2010  
Stations 20 and 25

Profile of ocean properties collected with CTD



CDOM – colored dissolved organic matter – showed obvious *anomaly* at depth (this profile shows the largest values measured).

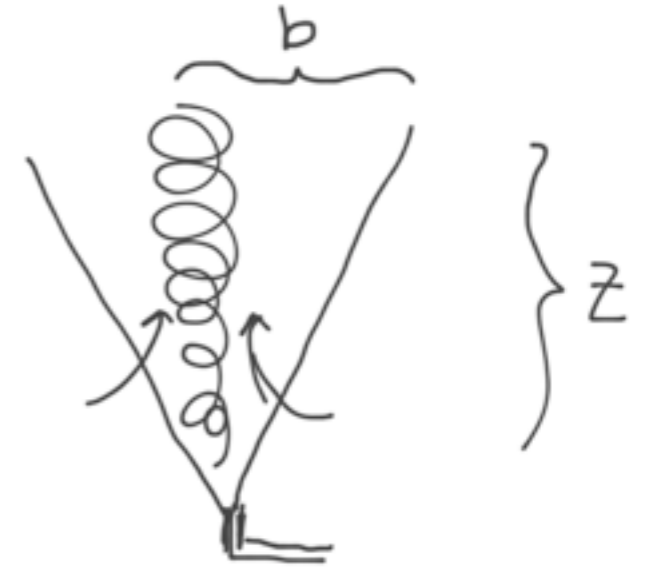
JAG, 2010

# Integral Models: Morton, Taylor, Turner, 1953

$$\frac{d(b^2 w)}{dz} = 2\alpha b w,$$

$$\frac{d(b^2 w^2)}{dz} = 2g\lambda^2 b^2 \theta,$$

$$\frac{d(b^2 w \theta)}{dz} = -\frac{1 + \lambda^2}{\lambda^2} \frac{d\epsilon}{dz} b^2 w$$



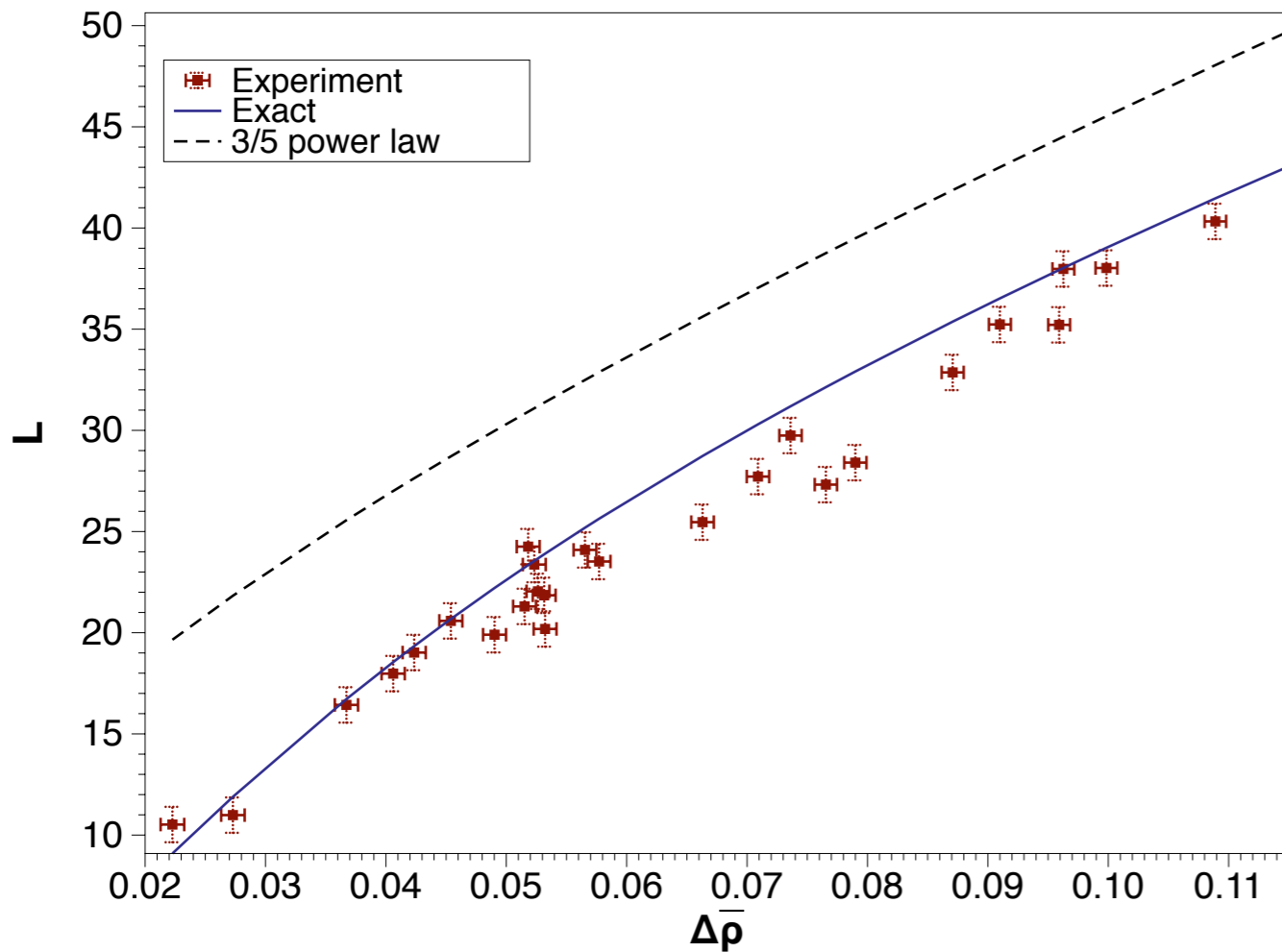
$\epsilon$  -- ambient stratification

$b, w, \theta$  -- jet radius, center speed, density

$\lambda, \alpha$  -- entrainment, mixing coefficients



# Miscible Limit: Critical Escape Height For Buoyant Jets



$$L = L_0 \int_1^A \frac{ds}{\sqrt{s^{5/4} + \epsilon - 1}}$$

$$\epsilon = \frac{5(1+\lambda^2)(\Delta\bar{\rho})r_0g}{16\sqrt{2}\alpha w_0^2} \quad A = (1 + \epsilon(\frac{\theta_0^2}{\theta_f^2} - 1))^{4/5}$$

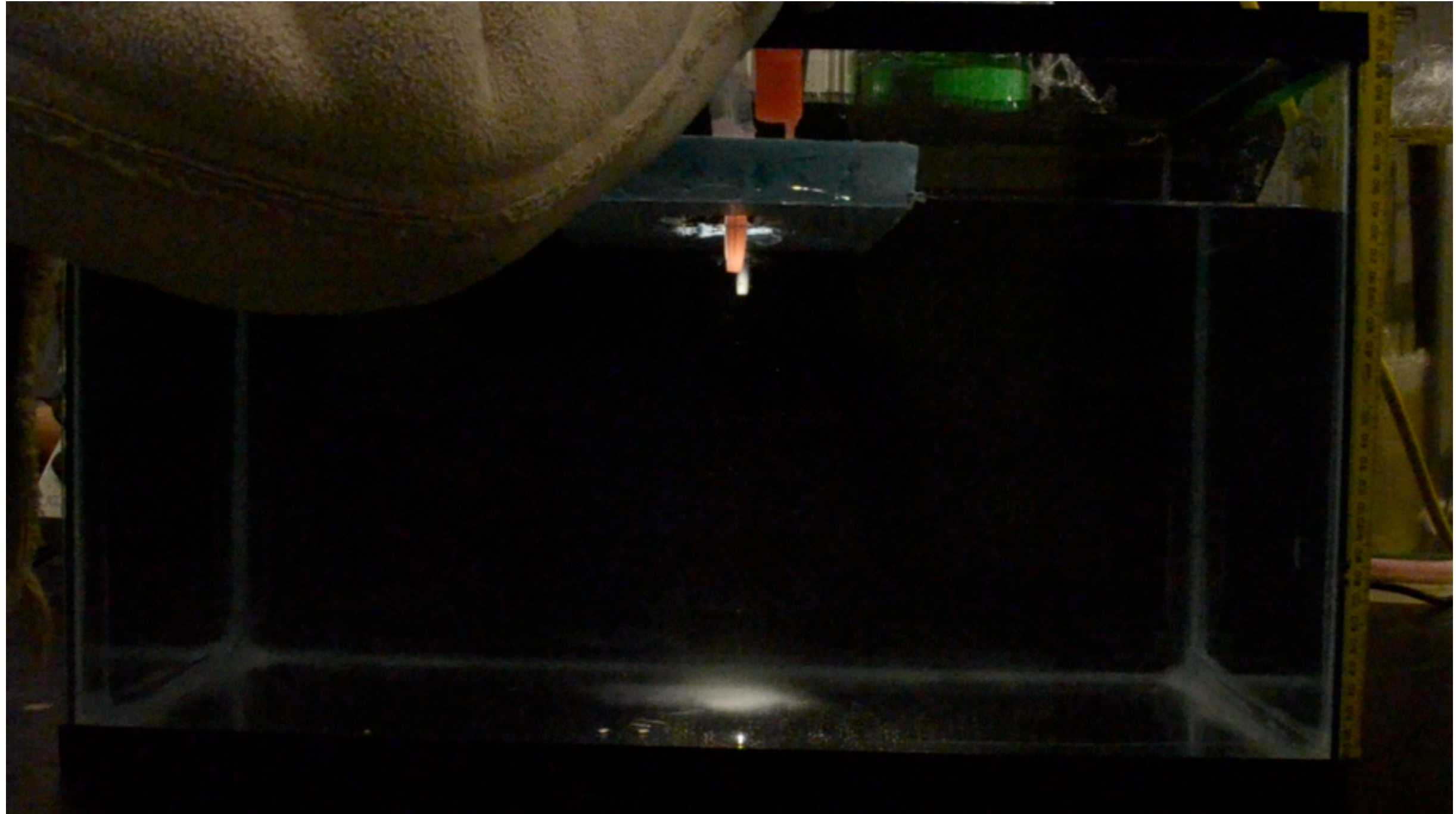
$$\theta_0 = \frac{(1+\lambda^2)}{\lambda^2} \Delta\bar{\rho} \quad \theta_f = \frac{\rho_b - \rho_t}{\rho_b} \quad \Delta\bar{\rho} = \frac{\rho_b - \rho_j}{\rho_b}$$

$$L_0 = \left( \frac{5r_0w_0^2}{16\sqrt{2}g(1+\lambda^2)\alpha(\Delta\bar{\rho})} \right)^{1/2}$$

Adalsteinsson, Camassa, Falcon, Lin, McLaughlin, Mertens, Nenon, Smith, Walsh, Watson, White,  
to appear: "Monitoring and Modeling the Deepwater Horizon Oil Spill:  
A Record-Breaking Enterprise, AGU Monograph Series

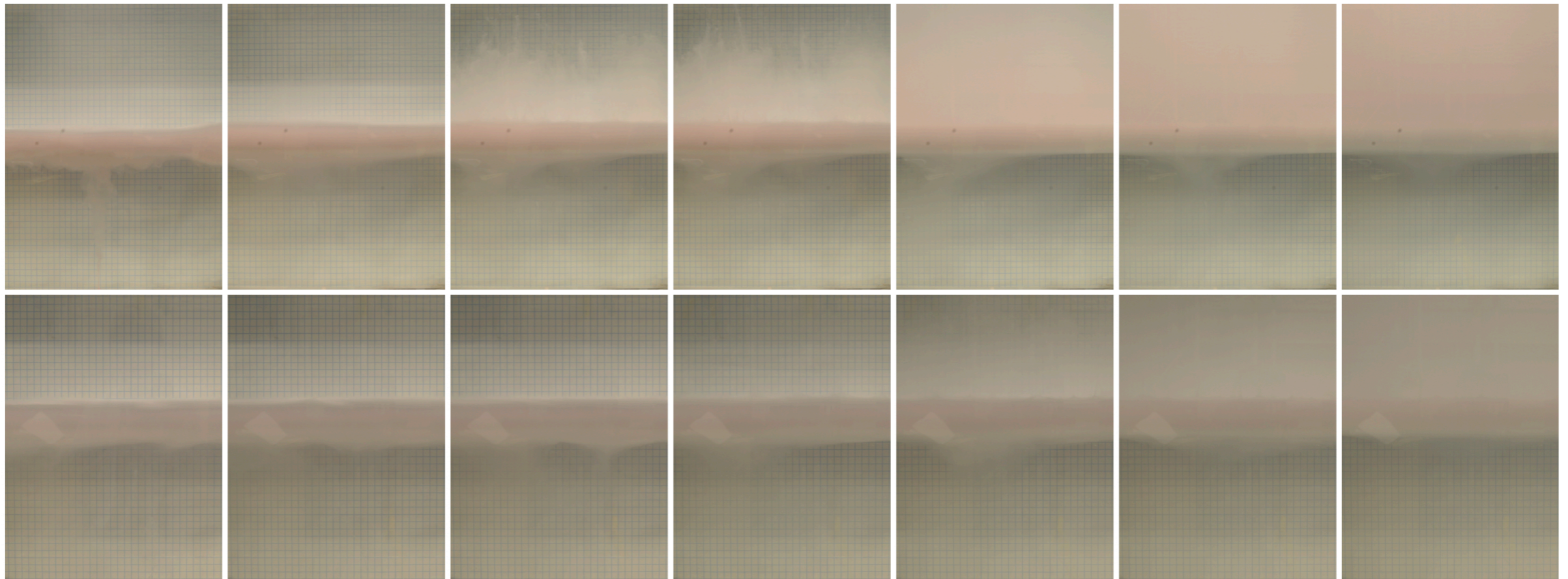
Asymptotics-- Camassa, McL, Tzou, Zhao, in prep

# Current Events: Ocean Carbon Pump





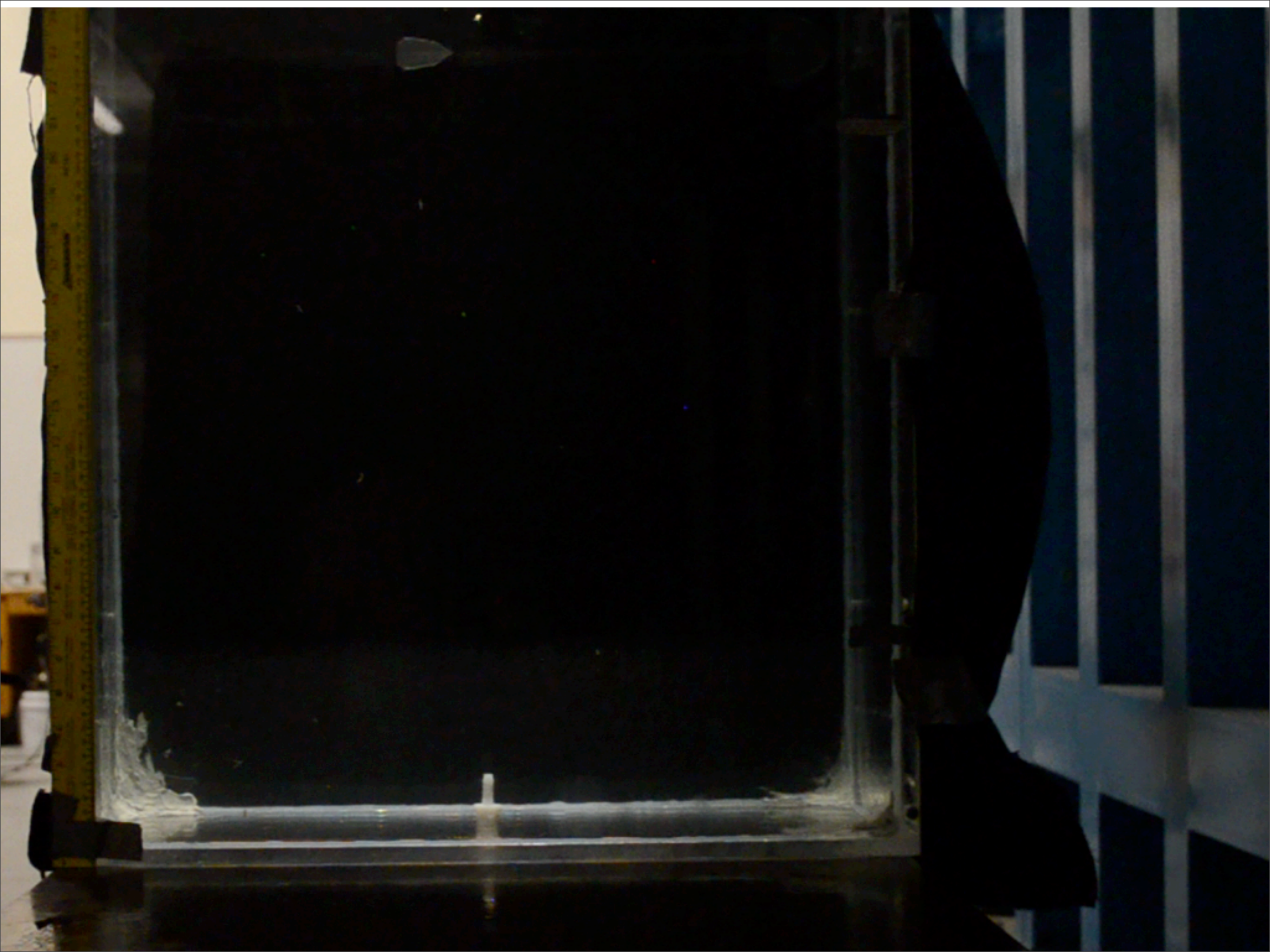
# Plume Destabilization



**Figure 3.** Time series showing timescale of plume instability. **Top:** OSW 4:3:2,  $t = 30, 450, 870, 900, 1800, 3600, 7200$  sec. **Bottom:** OSW 4:3:17,  $t = 30, 450, 900, 1800, 3600, 7200, 14400$  sec. Notice the onset of instability in the top row, first evident at  $t = 870$  sec.

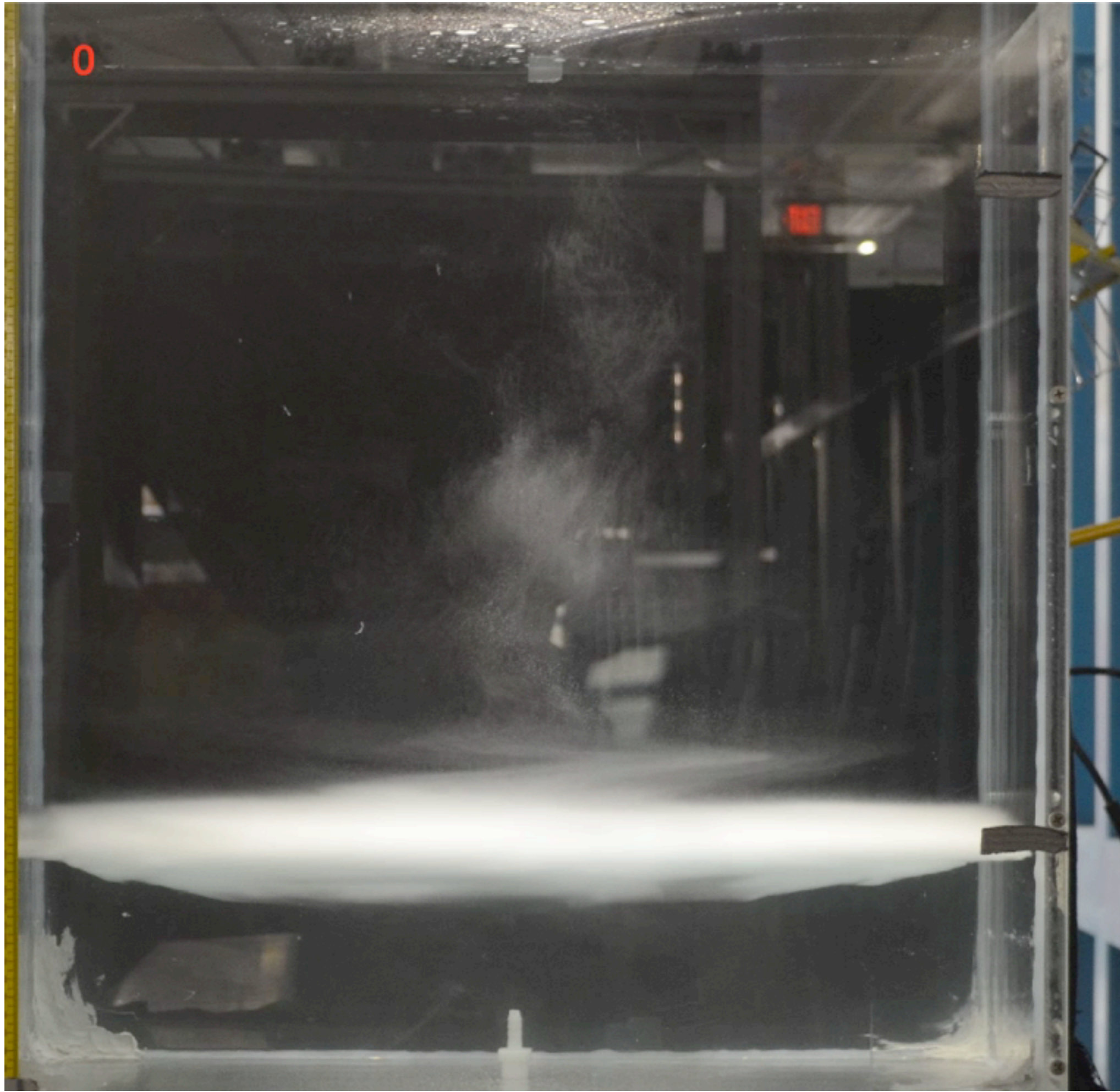








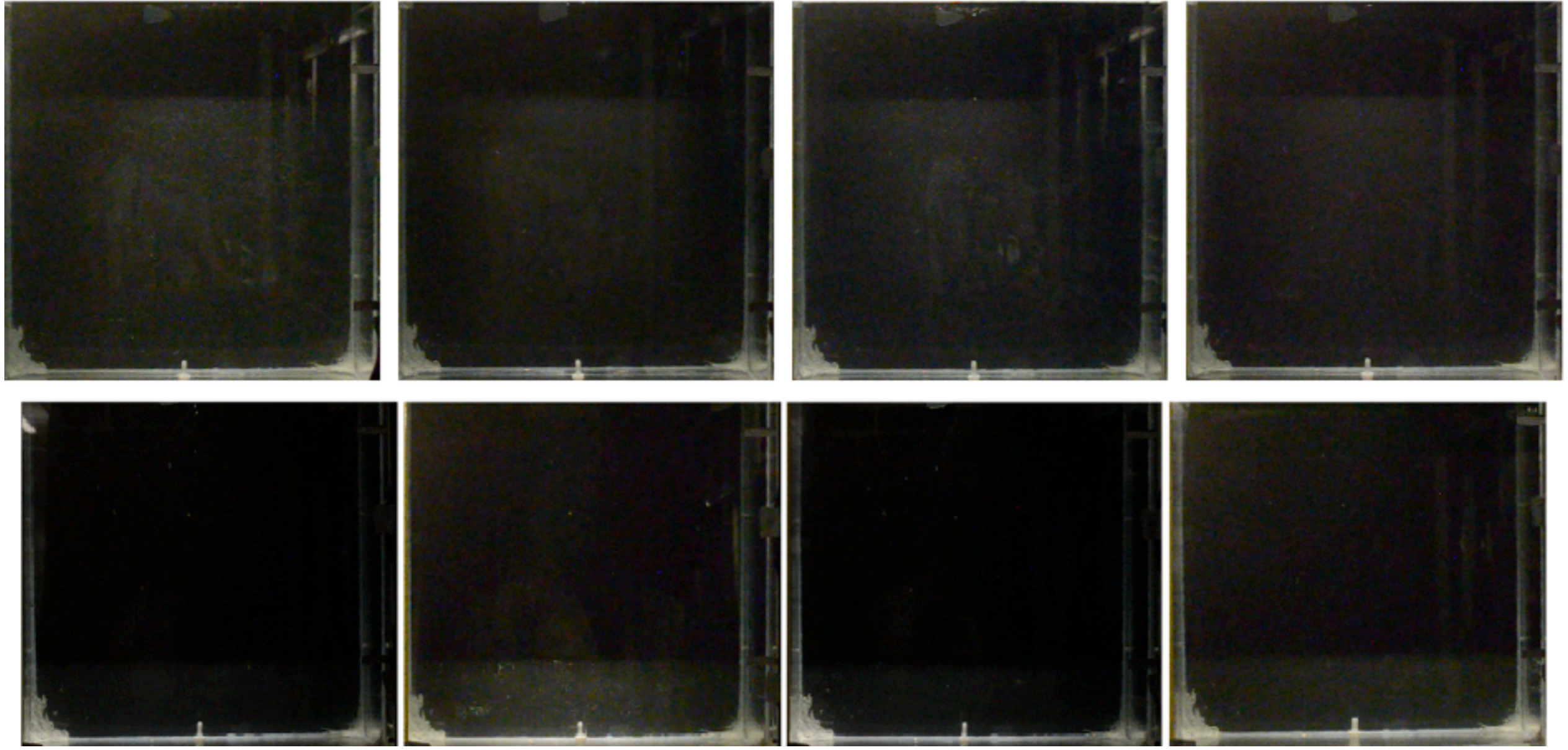




Top: 48 cm travel, Bottom 15cm  
Left to right: increasing flow rate



Top: 48 cm travel, Bottom 15cm  
Left to right: increasing flow rate



# Stratified Vortex Rings

Camassa, McL, **Keith  
Mertens**, D. Nenon, C.  
Smith, C.Viotti, in prep

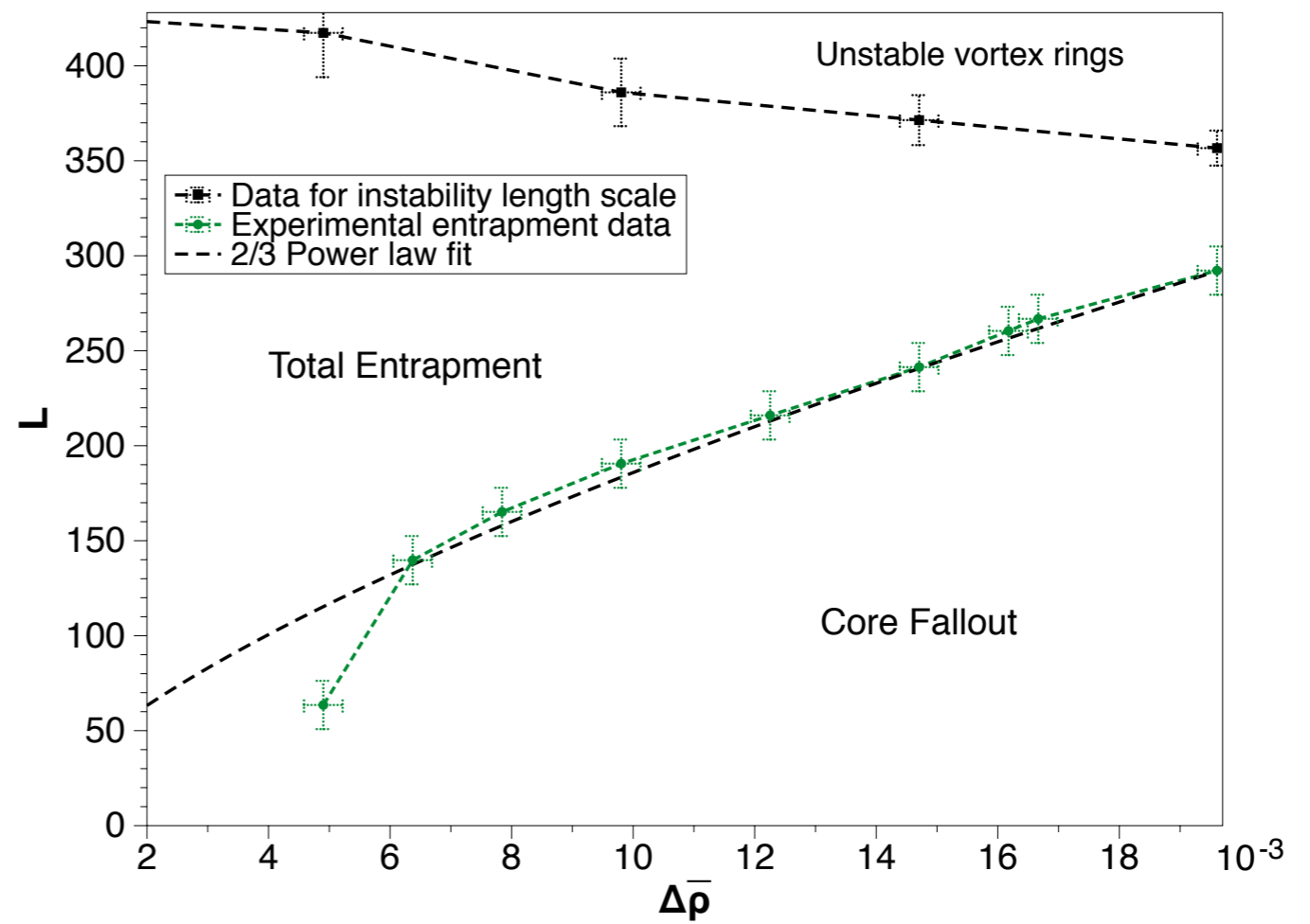


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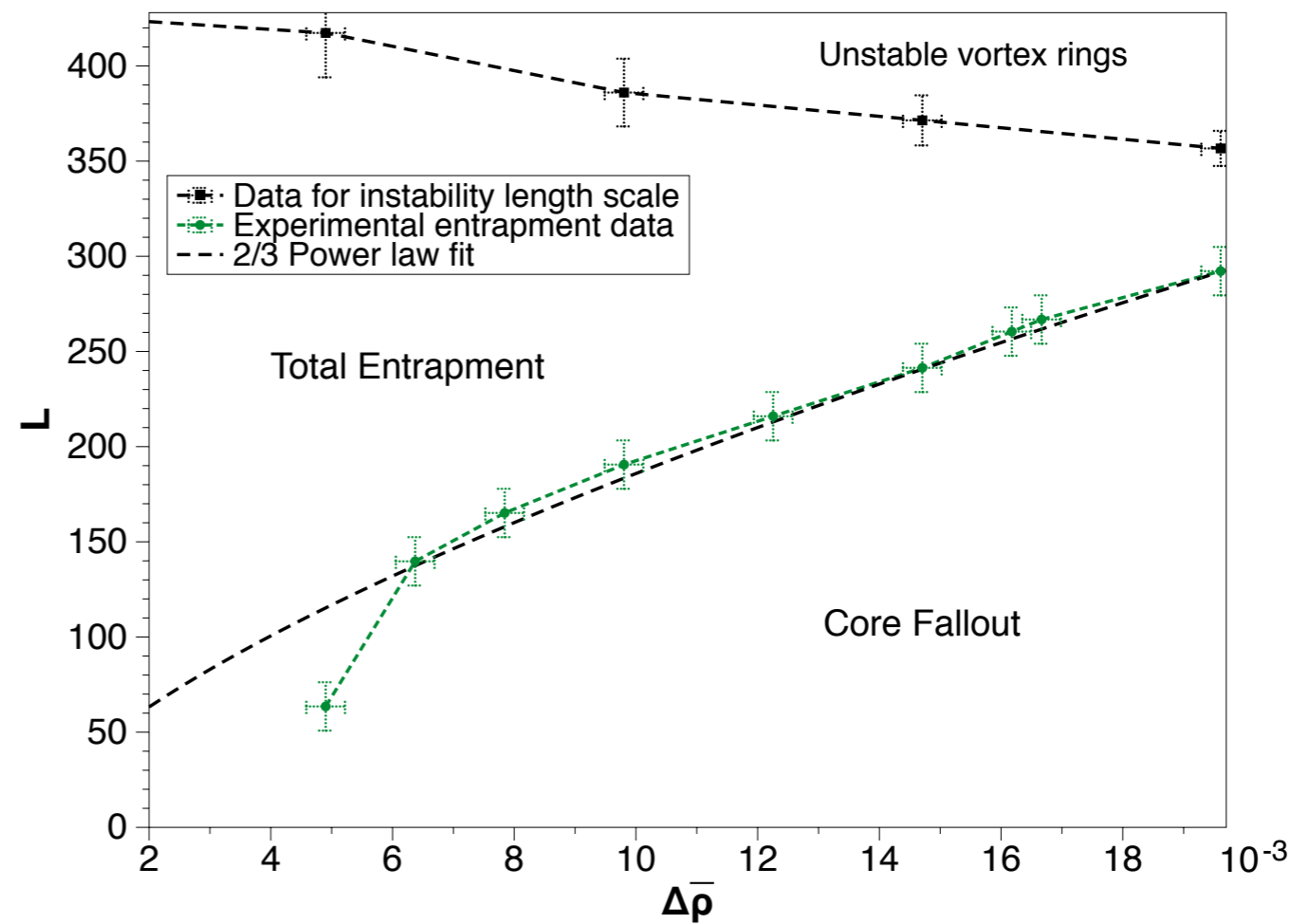
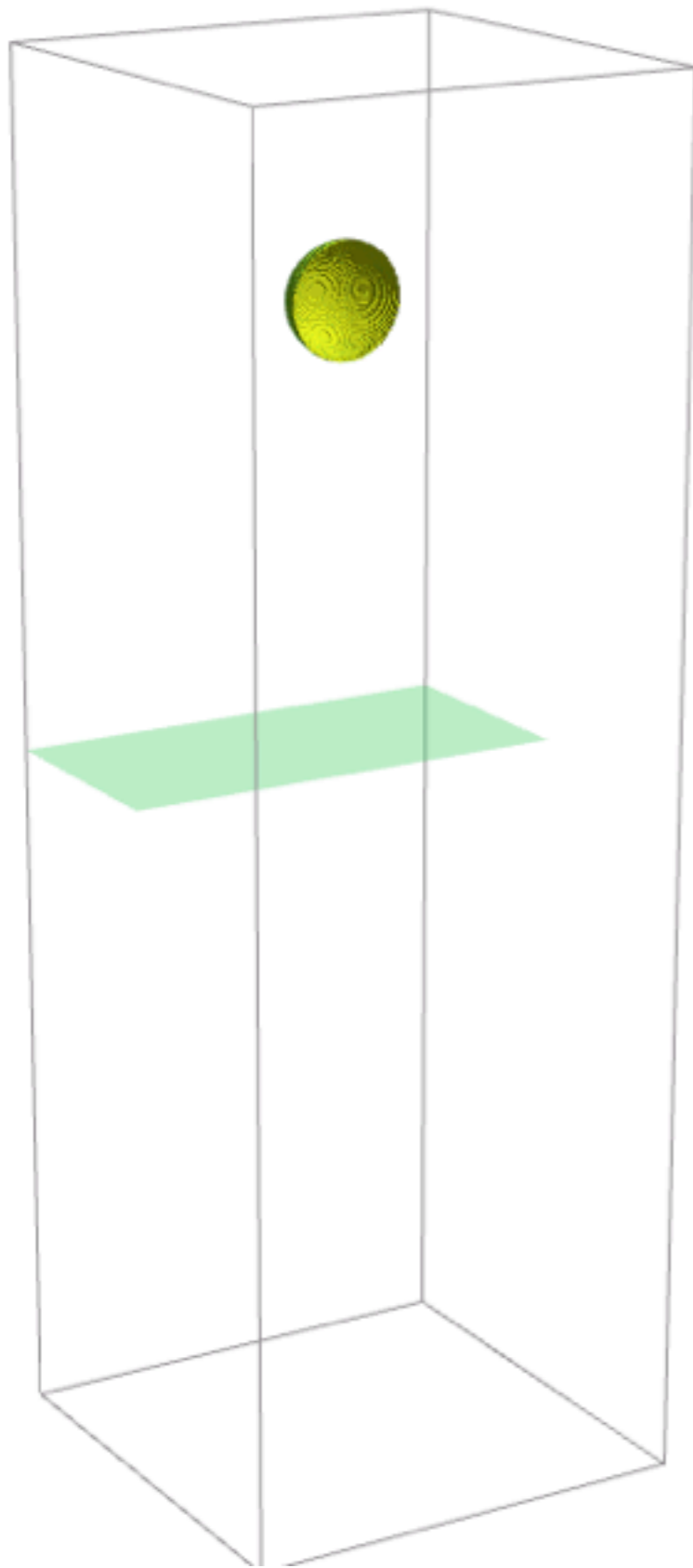
# DNS: Varden (A.Almgren LBL Code) modified by Claudio Viotti

mesh:256x256x1024,  
parallel on 256 processors  
run time: 6 hours  
periodic x-y, slip wall velocity lids  
no flux bc for scalar



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## Conclusions and Future:

Buoyant plume formation in stratification

Trapping timescales vary with mixture

Plume destabilization may occur

Internal waves-- larger scale experiments

Inflow full DNS CFD marginally resolvable



# UNC Joint Fluids Lab, Chapman Hall Level B, rm B02







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## Why Did Huge Oil Plumes Form After the Gulf Spill

Dispersants broke oil into micro-droplets suspended by equally dense water.



**Oil jets pre-mixed with soap are fired into layered fluid, mimicking the spreading of a Gulf oil plume.**

*Photograph by Steve Harenberg, Rich McLaughlin, Johnny Reis, William Schlieper, Will Owens, Brian White, UNC Joint Fluids Laboratory and UNC Center for Interdisciplinary Applied Mathematics Roberto Camassa/The University of North Carolina*



